

--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--

**VASAVI COLLEGE OF ENGINEERING (Autonomous), HYDERABAD**  
**B.E. (IT) III Year I-Semester Supplementary Examinations, May/June-2018**

**Theory of Automata**

Time: 3 hours

Max. Marks: 70

*Note: Answer ALL questions in Part-A and any FIVE from Part-B*

**Part-A (10 × 2 = 20 Marks)**

- Write the basic differences between a DFA and an NFA?
- Define regular expression and give two examples.
- State the pumping lemma for regular languages.
- What is a parse tree? Give one example.
- Construct a PDA equivalent to the following grammar.  
 $S \rightarrow aAA$   
 $A \rightarrow aS \mid bS \mid a$
- List the closure properties of context free languages.
- Describe Multi Stack Turing Machine?
- Write the formal definition of Turing Machine
- Define Modified Post's Correspondence Problem (MPCP).
- What is an NP Complete Problem?

**Part-B (5 × 10 = 50 Marks)**

- Construct an  $\epsilon$ -NFA for the regular expression  $(00 + 11) 0^*$  [4]
  - Convert the following  $\epsilon$ -NFA to NFA (without  $\epsilon$  transitions) [6]

	$\epsilon$	a	b	c
$\rightarrow p$	{q, r}	$\phi$	{q}	{r}
q	$\phi$	{p}	{r}	{p, q}
*r	$\phi$	$\phi$	$\phi$	$\phi$

- Minimization the following DFA. [6]

$\delta$	0	1
$\rightarrow A$	B	E
B	C	F
C	D	H
*D	E	H
E	F	I
F	G	B
G	H	B
H	I	C
*I	A	E

- Check whether the following grammar is ambiguous or not. [4]  
 $S \rightarrow aB \mid bA$   
 $A \rightarrow aS \mid bAA \mid a$   
 $B \rightarrow bS \mid aBB \mid b$

13. a) Design a PDA that accepts  $\{wcw^n \mid w \in (0+1)^*\}$  [5]  
 b) State pumping Lemma for Context-Free Languages and prove that the following Language is not Context free Language. [5]

$$\{0^n 1^n 2^n \mid n \geq 1\}$$

14. a) Design a Turing Machine to compute the proper subtraction function which is defined as below [7]  

$$m - n = m - n \text{ if } m \geq n$$

$$= 0 \text{ if } m < n$$

- b) Explain the halting problem of Turing machines. [3]

15. a) What is PCP and test whether the following PCP instance has a solution or not. [5]  
 $A = (ab, a, bc, c) \quad B = (bc, ab, ca, a).$

- b) Define universal language and write the binary code corresponding to the turing machine M whose moves are given as: [5]

$$\begin{aligned} \delta(q_1, 1) &= (q_3, 0, R) \\ \delta(q_3, 0) &= (q_1, 1, R) \\ \delta(q_3, 1) &= (q_2, 0, R) \\ \delta(q_3, B) &= (q_3, 1, L) \end{aligned}$$

16. a) Convert the following DFA to a regular expression using Arden's Theorem. [5]

$\delta$	a	b
$\rightarrow *P$	S	P
Q	P	S
R	R	Q
S	Q	R

- b) Show that  $\{0^i 1^j \mid \gcd(i, j) = 1\}$  is not regular. [5]

17. Answer any *two* of the following:

- a) Obtain a CFG that generates the language accepted by following PDA [5]  
 $M = ( \{q_0, q_1\}, \{a,b\}, \{A,Z\}, \delta, q_0, Z, \{q_1\} )$   
 with the transitions  $\delta(q_0, a, Z) = (q_0, AZ)$   
 $\delta(q_0, b, A) = (q_0, AA)$   
 $\delta(q_0, a, A) = (q_1, \epsilon)$

- b) Discuss about various modifications of Turing Machines. [5]

- c) Explain the SAT problem. [5]

XXXXXXXXXXXX